



M 26751

Reg. No. : .....

Name : .....

I Semester M.C.A. (Reg./Sup./Imp.) Degree Examination, February 2015  
(2013 and Earlier Admn.)

MCA C1.3 : DISCRETE MATHEMATICS

Time : 3 Hours

Max. Marks : 80

**Instruction :** Answer any five questions.

1. a) Show that  $(\sim p \wedge (\sim q \wedge r) \vee (q \wedge r) \vee (p \wedge r)) \Leftrightarrow r$ . 5
- b) Obtain the principle disjunctive normal form of  $(\sim p \vee \sim q) \rightarrow (\sim p \wedge r)$ . 5
- c) Define tautology. Show that  $((p \vee \sim q) \wedge (\sim p \vee \sim q)) \vee q$  is a tautology. 6
2. a) If A, B, C are sets then show that : 8
  - i)  $A \times (B \cup C) = (A \times B) \cup (A \times C)$
  - ii)  $A \times (B \cap C) = (A \times B) \cap (A \times C)$ .
- b) Define an equivalence relation. Let  $A = \{1, 2, 3, 4, 5, 6, 7\}$  and  $R = \{(x, y) \mid x - y \text{ is divisible by } 3\}$ . Show that R is an equivalence relation. Draw the graph of R and write its matrix. 8
3. a) Define the converse, inverse and contrapositive of a conditional statement. State the converse, inverse and contrapositive to the following statement. "If triangle ABC is a right angled triangle, then  $|AB|^2 + |BC|^2 = |AC|^2$ ". 6
- b) Find the selection of the recurrence relation  $a_n = a_{n-1} + 2a_{n-2}$ ,  $n \geq 2$  with the initial conditions  $a_0 = 1$  and  $a_1 = 8$ . 4
- c) Use mathematical induction to show that  $1 + 2 + 2^2 + \dots + 2^n = 2^{n+1} - 1$ . 6

P.T.O.



4. a) Let  $M_R = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$  and  $M_S = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix}$  be relation matrices of the

relations R and S respectively. Show that  $M_{R \circ S} = M_{S \circ R}$ .

- b) Define one-one and onto function. Give an example each.
- c) State Pigeonhole principle. How many people among 2,00,000 people are born at the same time (hour, minute, seconds) ?
5. a) Let  $f: A \rightarrow B$  and  $g: B \rightarrow C$  be both one-one and onto functions. Then show that  $g \circ f: A \rightarrow C$  is also one-one and onto.
- b) Show that :
- i)  $\binom{n+1}{r} = \binom{n}{r} + \binom{n}{r-1}$
- ii)  $r \cdot {}^n C_r = n \cdot {}^{(n-1)} C_{r-1}$ .
- c) Let  $A = \{1, 2, 3, 4, 12\}$ . Consider the partial order of divisibility on A. That is, if a and b are in A,  $a \leq b$  if and only if  $a|b$ . Draw the Hasse diagram of  $(A, \leq)$ .
6. a) Show that the set  $G = \{0, 1, 2, 3, 4\}$  is an abelian group with respect to addition modulo 5.
- b) State and prove Lagrange's theorem.
- c) Prove that the intersection of any two subgroups of G is again a subgroup of G.
7. a) State and prove the addition theorem of probability.
- b) A problem in Mathematics is given to three students whose chances of solving the problem are  $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ . What is the probability that the problem is solved ?
- c) Explain path, reachability and connectedness.

- a) Show that a t
- b) Using Krusk
- below.



- c) In a disj

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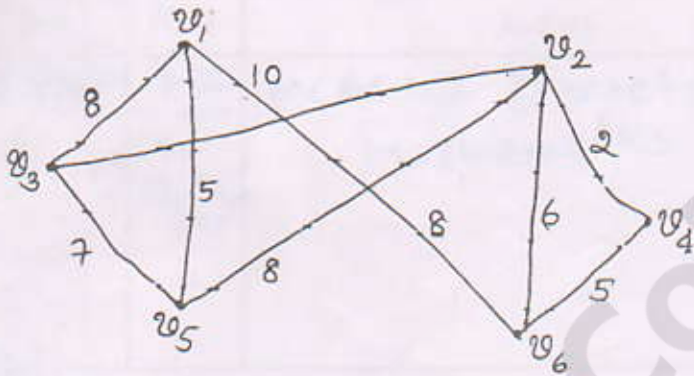
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6





- a) Show that a tree with  $n$  vertices has exactly  $(n - 1)$  edges. 6
- b) Using Kruskal's algorithm find the minimal spanning tree of the graph shown below. 5



- c) In a complete graph with  $n$  vertices prove that there are  $(n - 1)/2$  edge-disjoint Hamiltonian cycles, if  $n$  is an odd number  $\geq 3$ . 5

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